



GWL (GW + Wannier +Lanczos)

GWL hands-on

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Summary

- Calculation general structure (1): finite systems
METHANE molecule
 - minimal example
 - control of the polarizability basis
 - optimal representation of $|s\rangle$ vectors
 - number of lanczos iteration
- Calculation general structure (2): extended systems
Si bulk

Exercise: CO molecule

Calculation general structure (1): finite systems

pw.x: self-consistent calculation



pw4gww.x: prepare matrices



gww.x: compute GW corrections

Methane

step 1: scf calculation

```
&control
  calculation = 'scf',
  restart_mode='from_scratch',
  prefix='ch4',
  tprnfor = .true.,
  pseudo_dir = '../Pseudo//',
  outdir='./..'
/
&system
 ibrav= 1,
  celldm(1) =15.0,
  nat=5,
  ntyp= 2,
  ecutwfc =40.0,
  nbnd=5
/
&electrons
  diagonalization='cg'
  mixing_beta = 0.5,
  conv_thr = 1.0d-8
/
ATOMIC_SPECIES
H 1.0 H.pz-vbc.UPF
C 12.0 C.pz-vbc.UPF
ATOMIC_POSITIONS {bohr}
H 1.198204546 1.198204546 1.198204546
H -1.198204546 -1.198204546 1.198204546
H 1.198204546 -1.198204546 -1.198204546
H -1.198204546 1.198204546 -1.198204546
C 0.000000000 0.000000000 0.000000000
```

Gamma-point
calculation

./run_scf

Methane

step 1: scf calculation

```
&control
  calculation = 'scf',
  restart_mode='from_scratch',
  prefix='ch4',
  tprnfor = .true.,
  pseudo_dir = '../Pseudo//',
  outdir='./..'
/
&system
 ibrav= 1,
  celldm(1) =15.0,
  nat=5,
  ntyp= 2,
  ecutwfc =40.0,
  nbnd=5
/
&electrons
  diagonalization='cg'
  mixing_beta = 0.5,
  conv_thr = 1.0d-8
/
ATOMIC_SPECIES
H 1.0 H.pz-vbc.UPF
C 12.0 C.pz-vbc.UPF
ATOMIC_POSITIONS {bohr}
H 1.198204546 1.198204546 1.198204546
H -1.198204546 -1.198204546 1.198204546
H 1.198204546 -1.198204546 -1.198204546
H -1.198204546 1.198204546 -1.198204546
C 0.000000000 0.000000000 0.000000000
```

Gamma-point
calculation

```
./run_scf
```

```
> grep 'hest' methane_scf.out
```

```
> highest occupied, lowest
```

```
> unoccupied level (ev):
```

```
> -9.1111 -0.5651
```

Methane

step 2: pw4gww.x

```
./run_pw4gww
```

```
&inputpw4gww
  prefix='ch4'
  num_nbndv(1)=4
  num_nbnds=5
  l_truncated_coulomb=.true.
  truncation_radius=7.5d0
  numw_prod=50
  pseudo_dir = '../Pseudo//',
  outdir='./tmp/'
/
```

Valence band number

Total number of KS states

Use of truncated Coulomb interaction

Dimension of the polarizability basis

Methane

step 3: gww.x

```
&inputgww  
ggwin%prefix='ch4'  
ggwin%max_i=5,  
ggwin%i_min=1  
ggwin%i_max=5  
ggwin%omega=20  
ggwin%n=118,  
ggwin%grid_freq=5  
ggwin%second_grid_i=3  
ggwin%second_grid_n=10  
ggwin%omega_fit=20  
ggwin%n_grid_fit=240  
ggwin%n_fit=120,  
ggwin%n_multipoles=2  
ggwin%l_truncated_coulomb=.true.  
ggwin%outdir='./tmp'  
/
```

Total number of KS states

From state i_{\min} to state i_{\max}

Length of imaginary frequency grid

Number of grid points

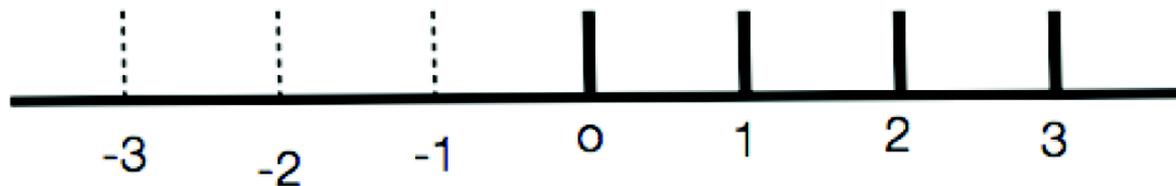
Grid kind and settings

Fit grid and number of points

Number of poles for the multipole expansion

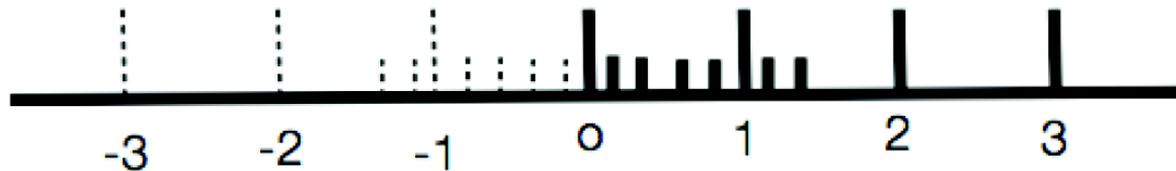
gww.x frequency grids

Equally spaces grid: \longrightarrow `ggwin%grid_freq=3`



Augmented at low
frequencies:

\longrightarrow `ggwin%grid_freq=5`
`ggwin%second_grid_i=1`
`ggwin%second_grid_n=2`



gww.x results

methane_gww.out:

- restart points
- qp corrections

```
QUASI-PARTICLES ENERGIES IN Ev, Spin:      1      1
State:    1DFT : -16.61262 GW-PERT : -20.45071 GW : -20.21650 HF-pert : -25.31702
State:    2DFT : -9.11175 GW-PERT : -13.67373 GW : -13.58907 HF-pert : -14.42319
State:    3DFT : -9.11175 GW-PERT : -13.67404 GW : -13.58654 HF-pert : -14.42319
State:    4DFT : -9.11175 GW-PERT : -13.67818 GW : -13.59240 HF-pert : -14.42319
State:    5DFT : -0.56520 GW-PERT :  0.21353 GW :  0.21301 HF-pert :  0.90042
```

IMAGINARY ENERGIES IN Ev:

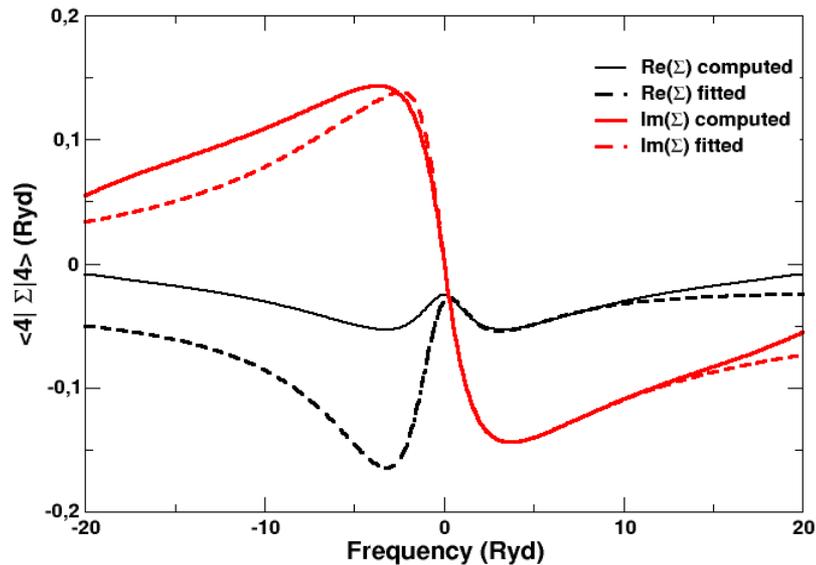
```
State:    1 GW (Im) :  0.48380
State:    2 GW (Im) : -0.04378
State:    3 GW (Im) : -0.05230
State:    4 GW (Im) : -0.04675
State:    5 GW (Im) :  0.02237
```

gww.x

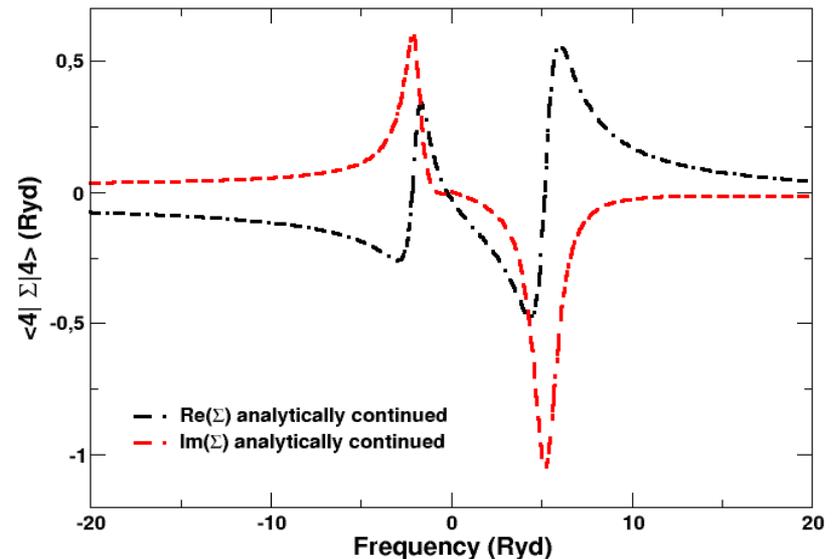
analytic continuation

`re_on_imXXXXX` and `im_on_imXXXXX`:

contain the expectation value of the self energy on the imaginary frequency axis (computed and fitted) and on the real axis.



COMPUTED AND FITTED ON
IMAGINARY AXIS



ANALYTICALLY CONTINUED ON
REAL AXIS

GWL results: methane ionization potential

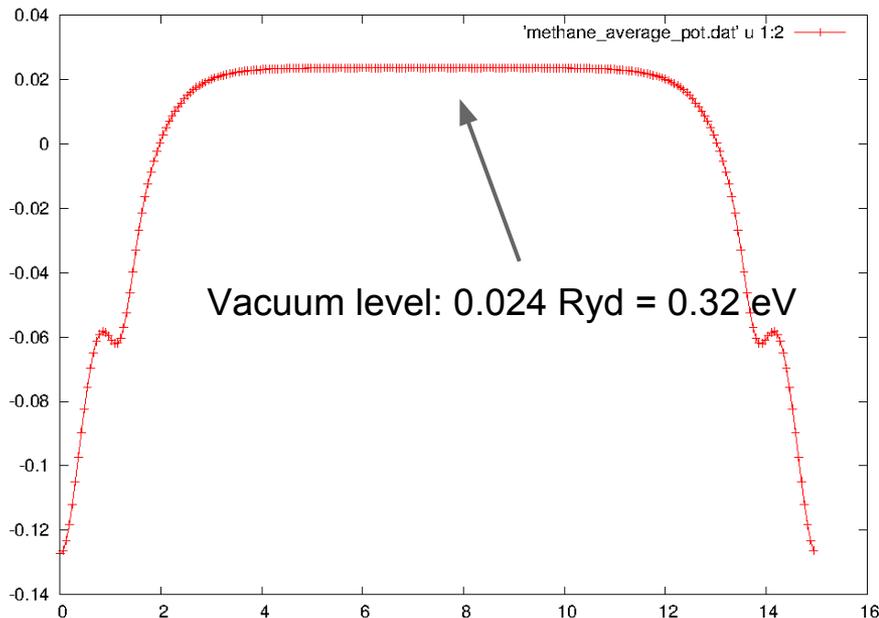
1) Get the vacuum level

```
run_vacuum
```

```
gnuplot
```

```
gnuplot> p 'methane_average_pot.dat' u 1:2 w lp
```

2) Compute the distance between the HOMO level and the vacuum level for the DFT and GW calculations.



IP

EXP: 12.6-13.6 eV

DFT: 9.4 eV

GW: 13.9 eV

GWL convergence (1): polarizability basis

$$P(i\omega) \simeq \sum_{\alpha\beta} \phi_{\alpha}(r) P_{\alpha\beta}(i\omega) \phi_{\beta}(r') \quad \{\phi_{\alpha}(r)\}$$

1) Consider “fake” conduction states, namely: planewaves below a certain threshold (`pmat_cutoff`) projected onto the conduction manifold.

$$P_0(t=0) = \sum_{vG} |\Psi_v \tilde{G}\rangle \langle \tilde{G} \Psi_v| \quad |\Psi_v \tilde{G}\rangle \longrightarrow |w_v \tilde{G}\rangle$$

2) Gram-Schmidt orthonormalize $\{|w_v \tilde{G}\rangle\}$ and keep the vectors $\{|f_{\mu}\rangle\}$ whose norm is above a certain threshold `s_pmat`.

$$P_{\mu\nu} = \sum_{vG} \langle f_{\mu} | \Psi_v \tilde{G}\rangle \langle \tilde{G} \Psi_v | f_{\nu}\rangle$$

4) Diagonalize $P_{\mu\nu}$ and keep the `numw_prod` eigenvectors with the largest eigenvalues.

Relevant input variables: `pmat_cutoff`, cutoff for the plane waves; `s_pmat` threshold for the f-states; `numw_prod` dimension of the final basis set.

GWL convergence (1): polarizability basis

```
./run_pol_basis
```

```
methane_pw4gww.in:  
  
&inputpw4gww  
  prefix='ch4'  
  num_nbndv(1)=4  
  num_nbnds=5  
  l_truncated_coulomb=.true.  
  truncation_radius=7.5d0  
  numw_prod= 150  
  pmat_cutoff= 5  
  pseudo_dir = './Pseudo//',  
  outdir='./tmp/'  
  
/
```

Final dimension of the
polarizability basis N_p

Cutoff E^* for the fake-
conduction state

GWL convergence (1): polarizability basis

How is the basis built?

(1) The fake conduction states are built depending on the cutoff E^*

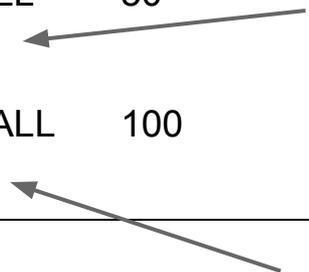
```
grep 'Number of projected orthonormalized plane waves:' *pw*out*
```

```
methane_pw4gww.out_pmc3_nwp100: Number of projected orthonormalized plane waves:      305
methane_pw4gww.out_pmc5_nwp50: Number of projected orthonormalized plane waves:      619
```

(2) the fake conduction states are multiplied by valence bands max. localized wannier functions and the $|f\rangle$ states are built depending on s_{pmat} . The total number of $|f\rangle$ states should be 4 times the dimension of the polarizability basis.

```
grep -A1 'NUMW_PROD_ALL' *pw*out*
```

```
methane_pw4gww.out_pmc3_nwp50: NUMW_PROD_ALL      50
methane_pw4gww.out_pmc3_nwp50- ATT1      282
--
methane_pw4gww.out_pmc5_nwp100: NUMW_PROD_ALL     100
methane_pw4gww.out_pmc5_nwp100- ATT1     471
```



GWL convergence (1): polarizability basis

How is the basis accurate?

(1) We keep only the polarizability eigenvectors with N_p largest eigenvalues. q^* is the value of the smallest eigenvalue under consideration. To compare calculations on different systems it should be normalized to the cell volume.

```
grep 'POLARIZABILITY eigen:      1' *out*
```

```
pmc3_nwp20: POLARIZABILITY eigen:      1 22.999807219904774
pmc3_nwp50: POLARIZABILITY eigen:      1 2.7577385557053447
pmc3_nwp100: POLARIZABILITY eigen:     1 0.23889032126141180
pmc3_nwp150: POLARIZABILITY eigen:     1 6.1518891131824148E-002

pmc5_nwp20: POLARIZABILITY eigen:      1 51.141601472951244
pmc5_nwp50: POLARIZABILITY eigen:      1 9.1427460621212475
pmc5_nwp100: POLARIZABILITY eigen:     1 1.4549266992868131
pmc5_nwp150: POLARIZABILITY eigen:     1 0.46373813148015497
```

GWL convergence (1): polarizability basis

How is the basis accurate?

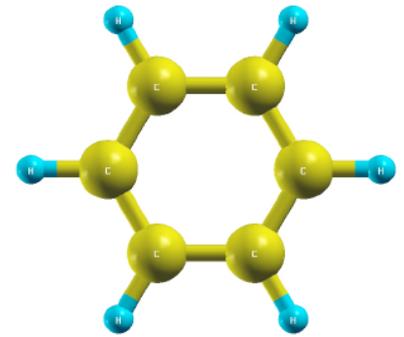
```
grep 'State: 4DFT' *out
```

then add 0.32 eV (vacuum level)

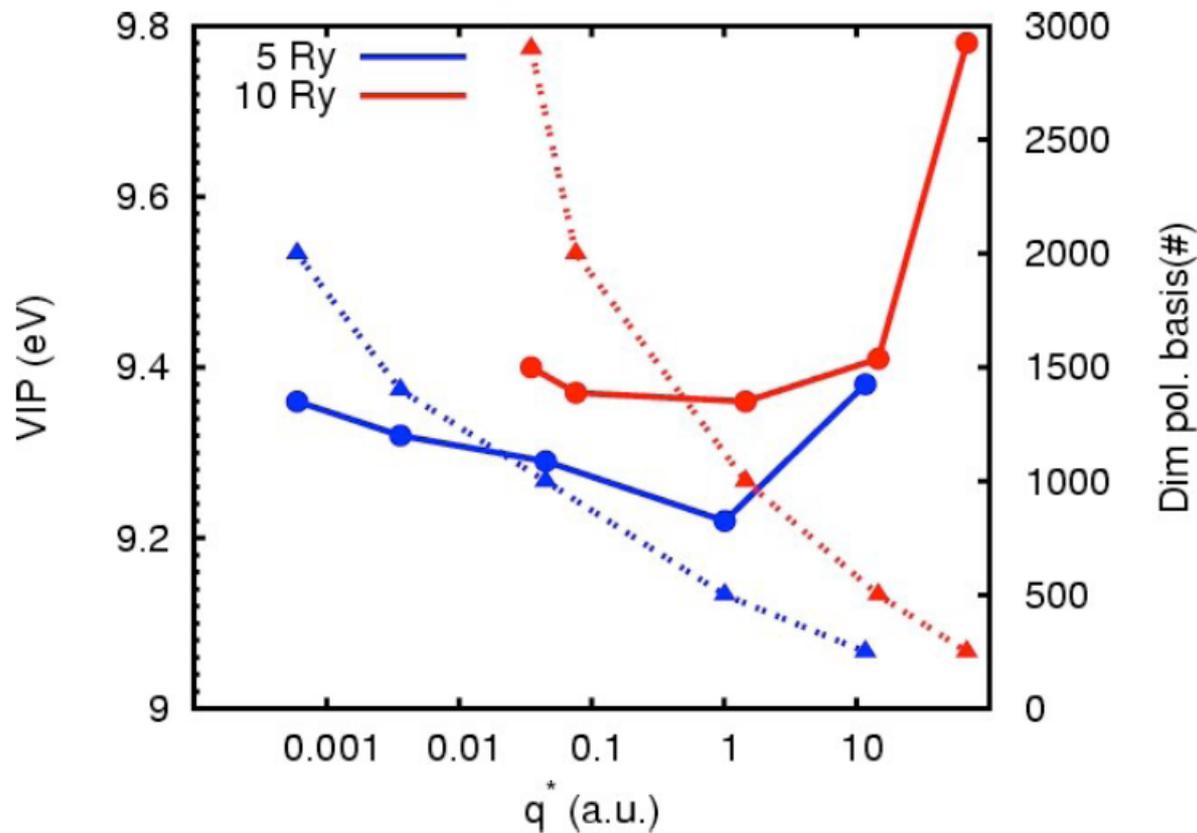
IP (eV)	Np=20	Np=50	Np=100	Np=150
E*= 3 Ryd	14.5	13.9	13.6	13.6
E*= 5 Ryd	14.3	14.2	13.9	13.8

EXP. IP
12.6-13.6 eV

GWL convergence (1): polarizability basis -benzene



convergence of first IP



GWL convergence (2):

optimal representation of large sets of vectors

- The Lanczos chain algorithm is applied twice to large sets of non-orthogonal vectors (to get the dynamical P, and for the calculation of the self-energy matrix elements, where the Green's function appear).

- An optimal representation of these vectors is found by:

- (1) 'Locally' diagonalizing the overlap matrix, keeping the eigenvectors with the largest `n_pola_lanczos`, or `n_self_lanczos` eigenvalues.

- (2) 'Globally' perform a SVD and keep the eigenvectors with the eigenvalue above `s_pola_lanczos` and `s_self_lanczos`.

In general we find a stronger system dependence for the s parameters.
(For a discussion see the GWL user manual)

GWL convergence (2):

optimal representation of large sets of vectors

```
./run_sself  
grep 'TOTAL NUMBER OF GLOBAL S VECTORS' *out*sself*
```

			IP (eV)
sself0.01:	TOTAL NUMBER OF GLOBAL S VECTORS:	1	14.7
sself0.00001:	TOTAL NUMBER OF GLOBAL S VECTORS:	50	13.8
sself0.000000001:	TOTAL NUMBER OF GLOBAL S VECTORS:	87	13.9
sself1d-12:	TOTAL NUMBER OF GLOBAL S VECTORS:	219	13.9

To notice the effect of `n_self_lanczos` increase the dimension of the polarizability basis.

```
./run_nself  
grep 'TOTAL NUMBER OF GLOBAL S VECTORS' *out*nself*
```

			IP (eV)
nself10:	TOTAL NUMBER OF GLOBAL S VECTORS:	50	13.1
sself50:	TOTAL NUMBER OF GLOBAL S VECTORS:	250	13.6
sself600:	TOTAL NUMBER OF GLOBAL S VECTORS:	377	13.6

GWL convergence (3): lanczos chain length

```
./run_nlanczos_self
```

```
&inputpw4gww  
  prefix='ch4'  
  num_nbndv(1)=4  
  num_nbnds=5  
  l_truncated_coulomb=.true.  
  truncation_radius=7.5d0  
  numw_prod= 50  
  pmat_cutoff= 3  
  pseudo_dir = '$PSEUDO_DIR',  
  outdir='$TMP_DIR'  
  n_pola_lanczos=400  
  s_pola_lanczos=0.5d0  
  nsteps_lanczos_pola=20  
  n_self_lanczos= 600  
  s_self_lanczos=1d-12  
  nsteps_lanczos_self= $nsteps  
  restart_gww=2  
  lanczos_restart=3
```

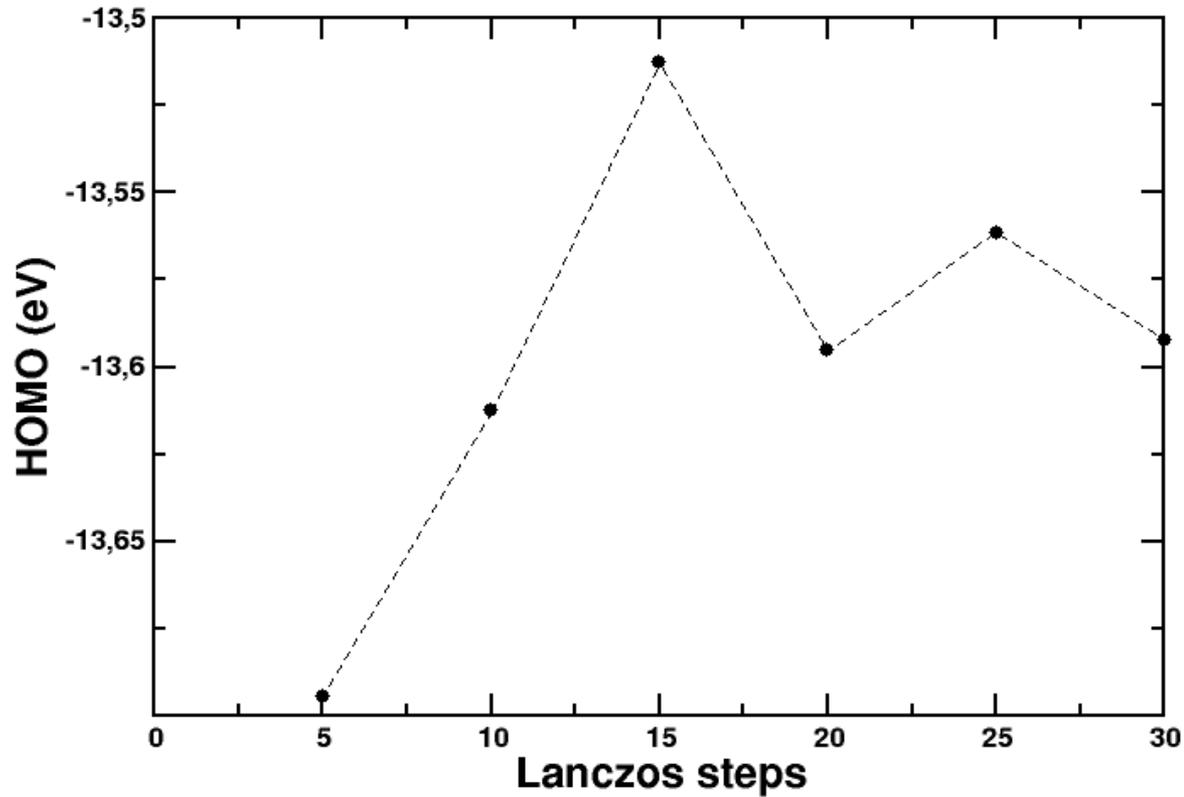
The code can be restarted to check the convergence with respect to to lanczos-chain length.

Increasing the number of steps

Restart points

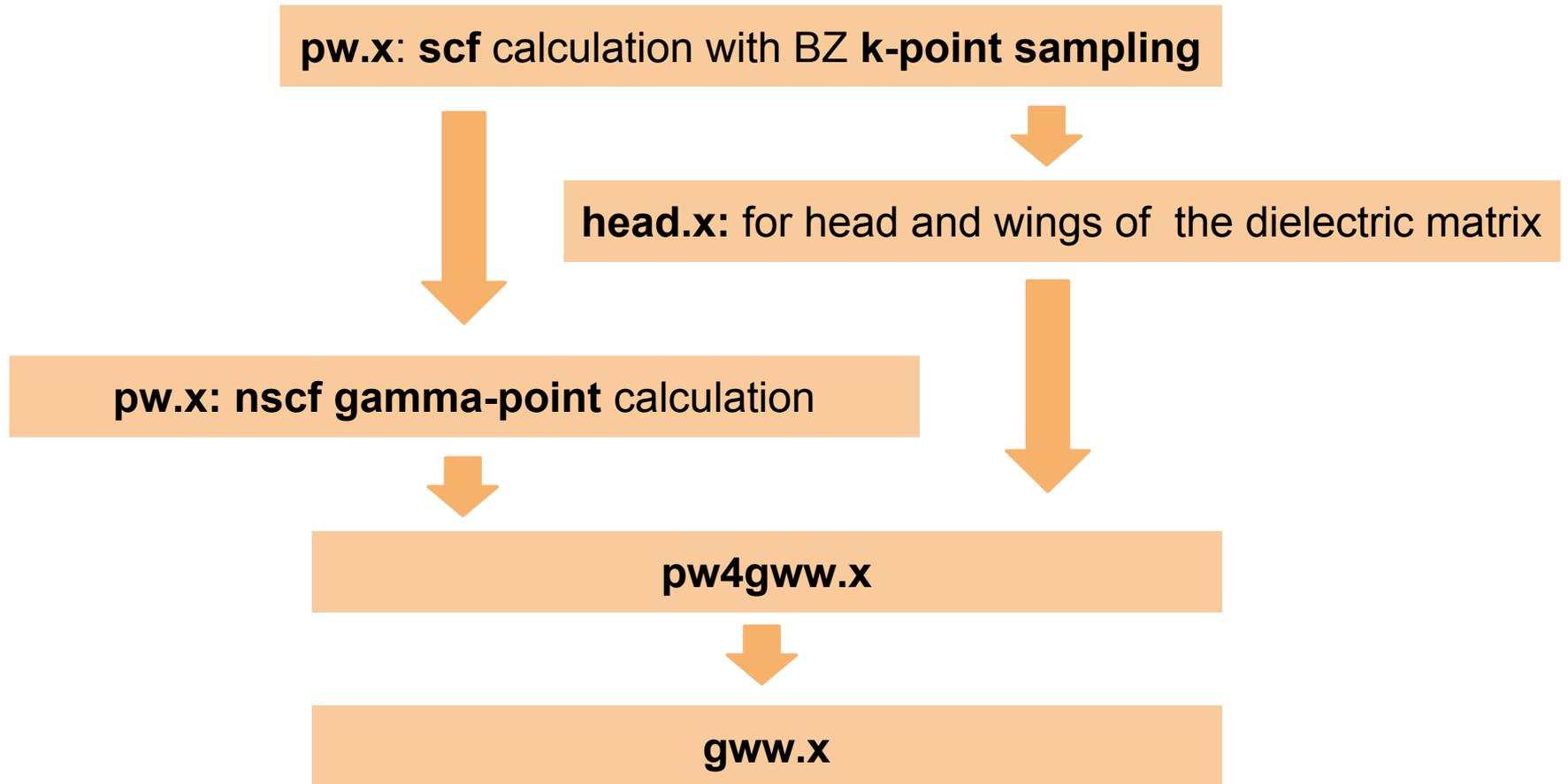
/

GWL convergence (3): lanczos chain length



Extended Systems

General Scheme (5 calculations)



Si-bulk

step 1 pw.x scf

```
&control
  calculation='scf'
  restart_mode='from_scratch', prefix='si'
  pseudo_dir = '$PSEUDO_DIR/',
  outdir='$TMP_DIR/'
/
&system
 ibrav= 8, celldm(1)= 10.26, celldm(2)= 1, celldm(3)=1,
  nat= 8, ntyp= 1, ecutwfc = 15.0
/
&electrons
  diagonalization='david',
  conv_thr = 1.0d-10,
  mixing_beta = 0.5,
  startingwfc='random',
/
ATOMIC_SPECIES
Si 1. Si.pz-vbc.UPF
ATOMIC_POSITIONS (crystal)
Si 0.00000 0.00000 0.00000
Si 0.50000 0.50000 0.00000
Si 0.00000 0.50000 0.50000
Si 0.50000 0.00000 0.50000
Si 0.25000 0.25000 0.25000
Si 0.75000 0.75000 0.25000
Si 0.75000 0.25000 0.75000
Si 0.25000 0.75000 0.75000
K_POINTS (automatic)
4 4 4 1 1 1
```

8 atom supercell.
THIS IS NOT CONVERGED!!!

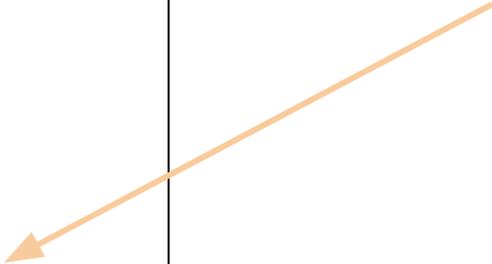
BZ K-point sampling

Si-bulk

step 2 head.x

```
calculation of head
&inputph
trans=.false.
l_head=.true.
tr2_ph=1.d-4,
prefix='si',
omega_gauss=20.0
n_gauss=97
grid_type=5
second_grid_i=1
second_grid_n=10
niter_ph=1
nsteps_lanczos=30
outdir='$TMP_DIR/'
/
0.0 0.0 0.0
```

Frequency grid parameters
Same as in gww.x input



Lanczos iteration number
Same as in gww.x input



Si-bulk

step 3-4: pw.x (nscf gamma) pw4gww.x

```
&control
  calculation='nscf'
  restart_mode='from_scratch',
  prefix='si'
  pseudo_dir = '$PSEUDO_DIR/',
  outdir='$TMP_DIR'
/
&system
 ibrav= 8, celldm(1)= 10.26,celldm(2)= 1, celldm(3)=1,
  nat= 8, ntyp= 1, ecutwfc = 15.0,nbnd=32
/
&electrons
  diagonalization='david', conv_thr = 1.0d-10,
  mixing_beta = 0.5,
  startingwfc='random',
/
ATOMIC_SPECIES
Si 1. Si.pz-vbc.UPF
ATOMIC_POSITIONS (crystal)
Si 0.00000 0.00000 0.00000
Si 0.50000 0.50000 0.00000
Si 0.00000 0.50000 0.50000
Si 0.50000 0.00000 0.50000
Si 0.25000 0.25000 0.25000
Si 0.75000 0.75000 0.25000
Si 0.75000 0.25000 0.75000
Si 0.25000 0.75000 0.75000
```

```
&inputpw4gww
  prefix='si'
  num_nbandv(1)=16
  num_nbands=32
  l_truncated_coulomb=.
false.
  numw_prod=100
  pmat_cutoff=3d0
  s_self_lanczos=1d-8
  outdir='$TMP_DIR'
/
```

Extended system

Si-bulk

step 3-4: pw.x (nscf gamma) pw4gww.x

```
&control
  calculation='nscf'
  restart_mode='from_scratch',
  prefix='si'
  pseudo_dir = '$PSEUDO_DIR/',
  outdir='$TMP_DIR'
/
&system
 ibrav= 8, celldm(1)= 10.26,celldm(2)= 1, celldm(3)=1,
  nat= 8, ntyp= 1, ecutwfc = 15.0,nbnd=32
/
&electrons
  diagonalization='david', conv_thr = 1.0d-10,
  mixing_beta = 0.5,
  startingwfc='random',
/
ATOMIC_SPECIES
Si 1. Si.pz-vbc.UPF
ATOMIC_POSITIONS (crystal)
Si 0.00000 0.00000 0.00000
Si 0.50000 0.50000 0.00000
Si 0.00000 0.50000 0.50000
Si 0.50000 0.00000 0.50000
Si 0.25000 0.25000 0.25000
Si 0.75000 0.75000 0.25000
Si 0.75000 0.25000 0.75000
Si 0.25000 0.75000 0.75000
```

```
&inputpw4gww
  prefix='si'
  num_nbandv(1)=16
  num_nbands=32
  l_truncated_coulomb=.
false.
  numw_prod=100
  pmat_cutoff=3d0
  s_self_lanczos=1d-8
  outdir='$TMP_DIR'
/
```

Extended system

You try, now!

Exercise:

-CO molecule

(1) DFT ionization potential

(2) convergence GW

Always check the convergence of your calculations!!

Important information can be found on the user manual, downloadable at the GWL-code web page.