

$$- \frac{d^2}{dx^2} \cos \frac{\pi x}{2L} + \frac{\pi^2}{4L^2} \cos \frac{\pi x}{2L} = 0$$

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2. Normalised wave function $\psi = A \cos\left(\frac{\pi x}{2L}\right)$

$$\langle \text{Kinetic energy} \rangle = -\frac{\hbar^2}{2m} \int_0^L \psi^* \nabla^2 \psi dx$$

$$= \frac{\hbar^2}{2m} \cdot \frac{\pi^2}{4L^2}$$

$$= \frac{\hbar^2 \pi^2}{8mL^2}$$

[1D finite well problem]

3. $\psi(r, t) = \psi(r) e^{-iEt/\hbar}$

$$P = \int \psi^* \psi d^3r$$

$$= \int \psi^*(r) \psi(r) e^{-i(E - E^*)t/\hbar} d^3r$$

$$\frac{\partial}{\partial t} P = -\frac{i}{\hbar} (E - E^*) \int \psi^* \psi e^{-\frac{i}{\hbar}(E - E^*)t} d^3r$$

$$= 0 \Rightarrow E = E^*$$