

# Assignment 10 - Metric Spaces, continuity

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1. Show that a function between metric spaces  $f : X \rightarrow Y$  is continuous at  $x \in X$  if and only if for every sequence  $(x_n)$  in  $X$  converging to  $x$ ,  $(f(x_n))$  converges to  $f(x)$ .
2. Show that a function  $f : X \rightarrow Y$  is continuous (i.e. continuous at all points of  $X$ ) if and only if for every open subset  $U \subset Y$ ,  $f^{-1}(U)$  is an open subset of  $X$ .